

# SGPE ECNM11049

## Advanced Time Series Econometrics

### Computer Tutorial 2

#### *Nonlinear Time Series Models*



#### Semester 2 Options

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### 1. The Threshold autoregressive (TAR) model

The file [Lab2data1.csv](#) contains monthly observations of the S&P500 stock market index from January 1959 through August 2016.

- (a) Construct a new variable which is the log difference of the stock price index. Graph the stock price index and its log difference. Use the log difference as your dependent variable,  $y_t$ , for the remaining parts of this question;
- (b) Look through the html file, run it and examine the output it produces;
- (c) While you are doing this, keep in mind the following facts and questions:
  - i. Estimate an AR(1) model for  $y_t$ . Calculate information criteria for this model;
  - ii. Estimate a homoskedastic TAR model for  $y_t$  using  $z_t = y_{t-1}$  as threshold trigger and  $\tau = 0$  as the threshold. Calculate information criteria for this model;
  - iii. Estimate a heteroskedastic TAR model for  $y_t$  using  $z_t = y_{t-1}$  as threshold trigger and  $\tau = 0$  as the threshold. Calculate information criteria for this model;
  - iv. Discuss your results. Is there evidence of threshold nonlinearity in this variable? If so, which parameters are changing across regimes?

### 2. The Markov switching model

In the lecture I went through an empirical example using a two regime Markov switching AR(1) model for US GDP growth (see the lecture slides for data definition, the data set is called [Lab2data2.csv](#)). I compared a homoskedastic variant of the model to a heteroskedastic one where the two regimes had different error variances and found strong evidence in favour of the latter.

- (a) Carry out a similar model selection exercise including a wider range of Markov switching models including:
  - i. models with 3 regimes,
  - ii. models with long lag lengths and
  - iii. models with regime switching only in the error variance (i.e. the AR coefficients and intercept are the same in all regimes). What is your preferred model?

- (b) For your preferred model, plot estimates of the probabilities that each time period falls in each regime. In the lecture slides, for the heteroskedastic model, I was able to interpret the two regimes as reflecting high and low variances. Can you offer a similar interpretation of the regimes for your preferred model? If not, how do you interpret your regimes?

### **3. Digression: A time-varying intercept model/unobserved component model**

The html file contains an example that explains in detail the mechanism of the Forward Filtering Backward Sampling (FFBS) algorithm. If you are ambitious, you may wish to take a look at this code.